



# From Lyon (1969) to Shanghai (2020), the International Congresses on Mathematical Education (ICME)

...as critical opportunities for crossing experiences of mathematics teaching and learning all over the world



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## 14<sup>th</sup> International Congress on Mathematical Education

July 12 to 19, 2020 Shanghai, China

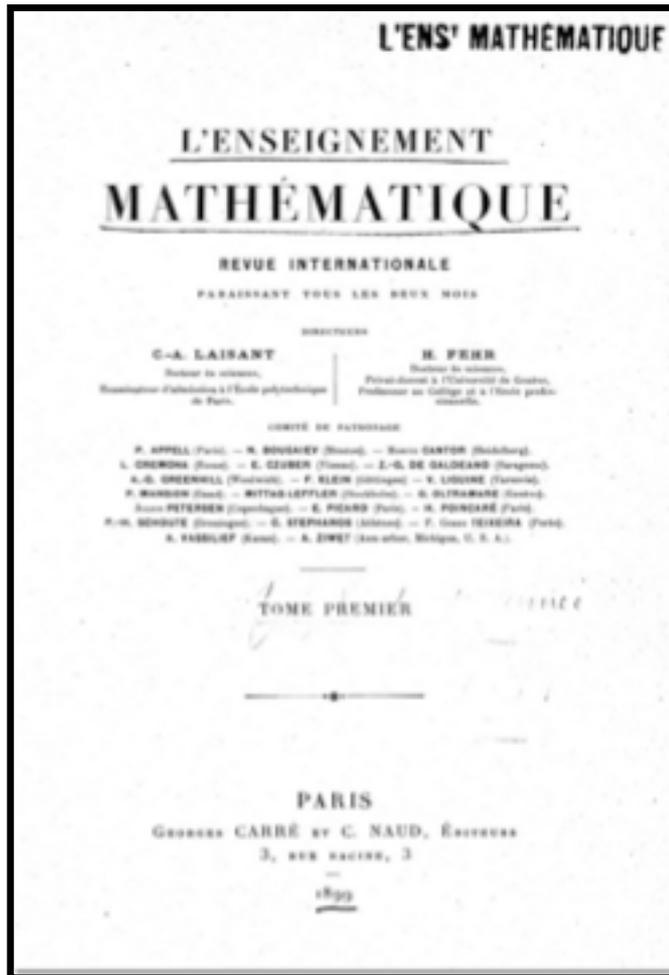


# Outlines

- 1) A short survey of ICME history, from Lyon 1969 and beyond
- 2) ICME experiences
- 3) Towards ICME-14, in ECNU Shanghai 2020
- 4) Current collaborative projects

# A short survey of ICME history

1899, Foundation of the journal “L’enseignement mathématique



The journal was founded in 1899 by Henri Fehr (Geneva) and Charles-Ange Laisant (Paris).

The objectives:

« associating the world of teaching to the huge movement of scientific solidarity emerging at the end of the XIXe century »

« Comparing the way of teaching mathematics in different countries »

Fehr was editor-in-chief until his death in 1954.

Online versions:

[http://www.unige.ch/math/EnsMath/EM\\_en/](http://www.unige.ch/math/EnsMath/EM_en/)

# A short survey of ICME history

## 1908, the birth of ICMI, some reasons of this birth

Regarding the French reform of 1902, the commission for designing the curricula in sciences was chaired by a mathematician (Gaston Darboux). Poincaré, Borel and Hadamard made lectures in the 'Musée pédagogique' for supporting its implementation

The International Commission on Mathematical Instruction (ICMI) was established at the Fourth International Congress of Mathematicians held in Rome in 1908. It was initiated to support a widespread interest among mathematicians in school education. The Rome Congress adopted a resolution, submitted on the initiative of the American mathematician, teacher, educator and historian of mathematics, David Eugene Smith (1860-1944), creating ICMI with the initial mandate of making a comparative study on the methods and plans of teaching mathematics at secondary schools.

<https://www.mathunion.org/icmi/organization/historical-sketch-icmi>

# A short survey of ICME history

1908, the birth of ICMI, its link to l'Enseignement mathématique



The idea of such an international commission had in fact been formulated by Smith himself three years earlier in the international journal *L'Enseignement Mathématique*, in his response to a survey proposed by the Editors on the "conditions to be satisfied by a complete — theoretical and practical — teaching of mathematics in higher institutions".

The initial ICMI mandate, an international comparative study, ultimately became a massive six-year project producing 187 volumes, containing 310 reports from eighteen countries.

The founding President of ICMI was the German mathematician Felix Klein (1849-1925). From the very beginning of ICMI, *L'EM* was adopted as its official organ, which is still the case today.

# A short survey of ICME history

1967, towards the Modern Math reform



Later ICMI presidents include such eminent mathematicians as Jacques Hadamard (from 1932 to the War),

After interruptions of activity around the two World Wars, ICMI was reconstituted in 1952. It was a time when the international mathematical community was being reorganized and ICMI then became an official commission of the International Mathematical Union (IMU). Successive presidents were Marshall H. Stone (1959-1962), then Lichnerowicz (1963-1966).

In 1967 the French government created the *Lichnerowicz Commission* made up of 18 teachers of mathematics. The commission recommended a curriculum based on set theory and logic with an early introduction to mathematical structures (“math modern reform”)

# A short survey of ICME history

1969, the birth of ICME



Hans Freudenthal, chairing ICMI from 1967 to 1970, had a view of mathematics, seen not primarily as a body of knowledge, but as a human activity, a view on mathematics education, seen essentially as a development from the concrete to the general, and a view on research on mathematics education to be developed as a new field, not restricted to a statistical or psychological point of view.

He drew all the consequences of such a position in creating a journal (Educational studies in Mathematics); a congress: the first ICME (International Congress on mathematical education) was launched in 1969 in Lyon, as a manifestation of independence from IMU; and an Institute: Freudenthal Institute in Utrecht (Bass 2008)

# A short survey of ICME history

1969, ICME, APM and IREM in Lyon

A convergence of mathematical evolution (the Bourbaki school), curricular reform (Modern Math), mathematics education as a research field (ICME) and deep social pressure (May 1968 events)

In 1968, at the time of the student demonstrations, Glaymann, mathematician in Lyon, president of the French national mathematics teacher association (APM), received an audience with the Minister of National Education, Edgar Faure and reiterates the APM proposition of creating IREM (Institutes for research on mathematics teaching)

Faure, after one week of reflection, to evaluate the cost of such an operation, proposed to create an IREM in Paris. Glaymann answered him that with the same budget, the APM thinks that three IREMs could be created.

This came to pass, Glaymann was named first director of the IREM at Lyon, and this, just in time, put him in a position to offer to host the first ICME in 1969 proposed by Freudenthal

# A short survey of ICME history

1985, creation of the ICMI studies



From 1983 to 1986, Jean-Pierre Kahane, a French mathematician, chaired ICMI. In 1985, he launched the *ICMI Studies*.

Each Study focuses on a topic or issue of prominent current interest in mathematics education. Built around an international conference, it is directed towards the preparation of a published volume intended to promote and assist discussion and action at the international, regional or institutional level.

The first one was, in 1985: *The Influence of Computers and Informatics on Mathematics and its Teaching*

The next one (ICMI Study 24): *School Mathematics Curriculum Reforms: Challenges, Changes and Opportunities*

<https://www.mathunion.org/icmi/activities/icmi-studies>

# A short survey of ICME history

2008, centennial of ICMI



A symposium was held in Rome to celebrate the 100th anniversary of this institution. It was addressed to a selected group of participants (150–200 people), under the title:

*The First Century of the International Commission on Mathematical Instruction (1908-2008) Reflecting and Shaping the World of Mathematics Education*

The programme included plenary sessions, invited short talks, and working groups. Most plenary lectures had a speaker and a reactor. Each working group had two leaders and up to 30 participants

For example, the WG « The role of resources and technology in mathematics education » (Maschietto & Trouche 2010)

<http://www.unige.ch/math/EnsMath/Rome2008/>

# ICME EXPERIENCES

# ICME-10 in Copenhagen



# Long trip

- Programme

- ✓ 8 days, from 9:00 to 20:00...

- Satellite conferences

- ✓ PME (International Group for the Psychology of Mathematics Education)

- ✓ HPM (History and Pedagogy of Mathematics)

- ✓ etc.

# ICME-11 in Monterrey (Mexico)



ICME 11

11th International  
Congress  
on  
Mathematical  
Education

Second Announcement

July 6th to 13th, 2006  
Monterrey, Mexico  
<http://icme11.org>



# What for? For whom?

Mathematicians

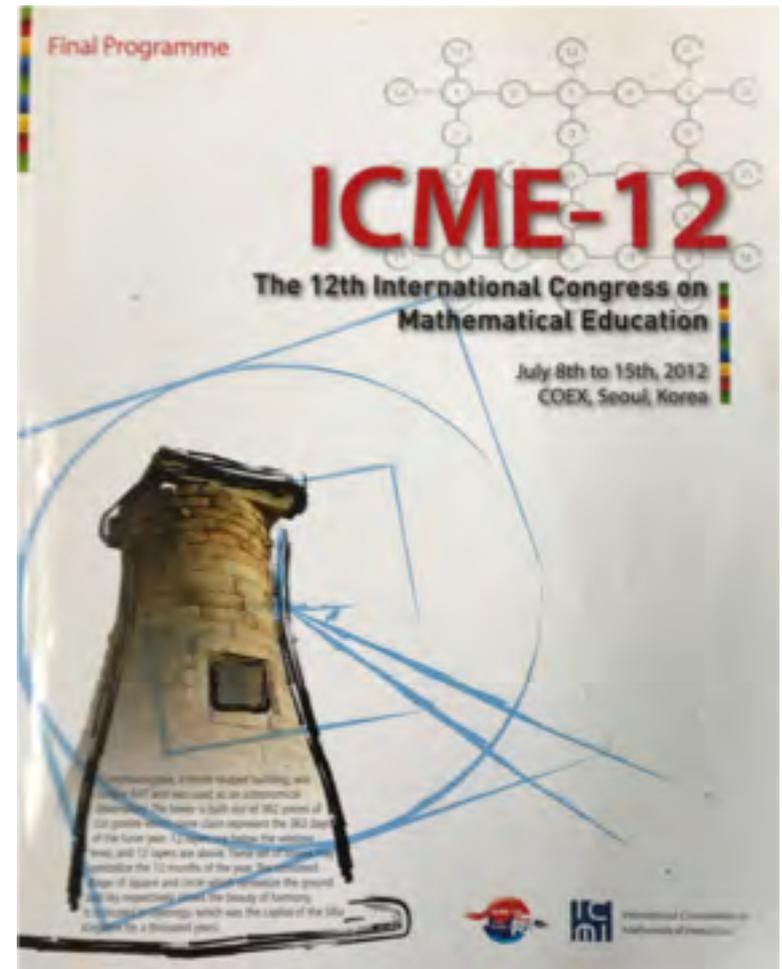
Researchers on  
math education

Teacher  
Educators

Teachers

Cross-cultural setting

# ICME-12 in Seoul (South Korea)



# ICMI and Japan

- ICME Participations

- ✓ Lyon (1969): 5/650; Exeter (1972): 40/1400; Karlsruhe (1976): 80/2000; etc.

- ICMI President

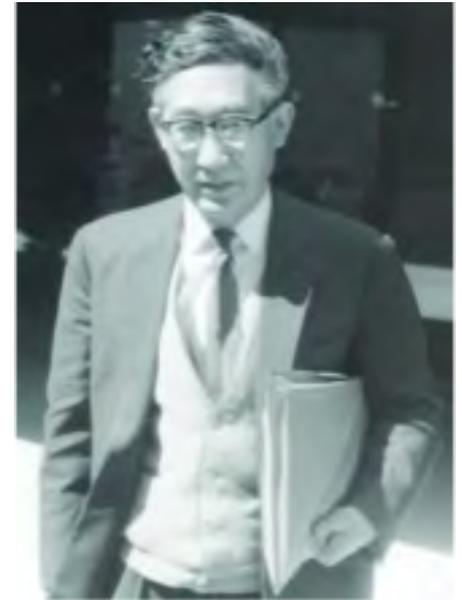
- ✓ 1975-1978: Shokichi Iyanaga

- ICME-9

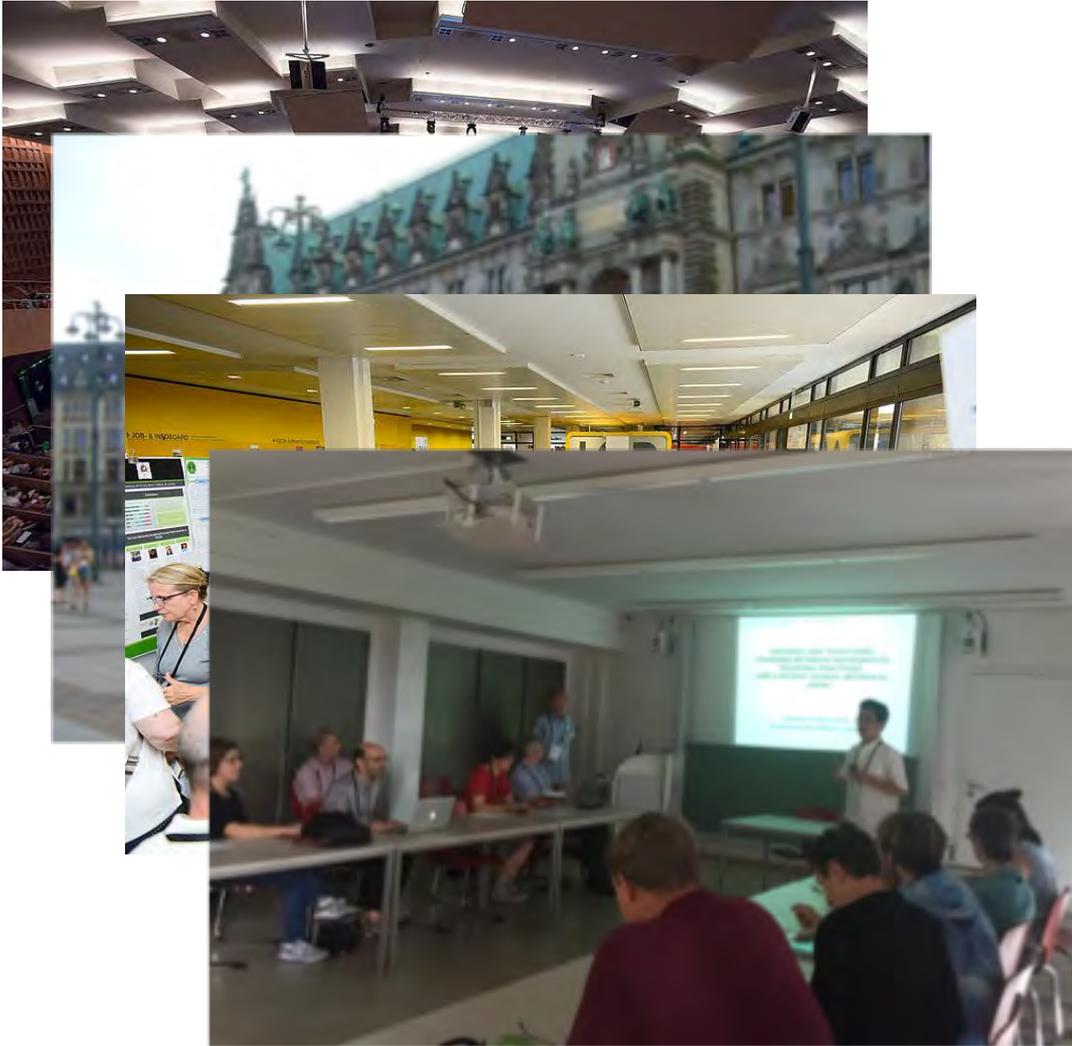
- ✓ Tokyo (Makuhari) in 2000

- IMU President

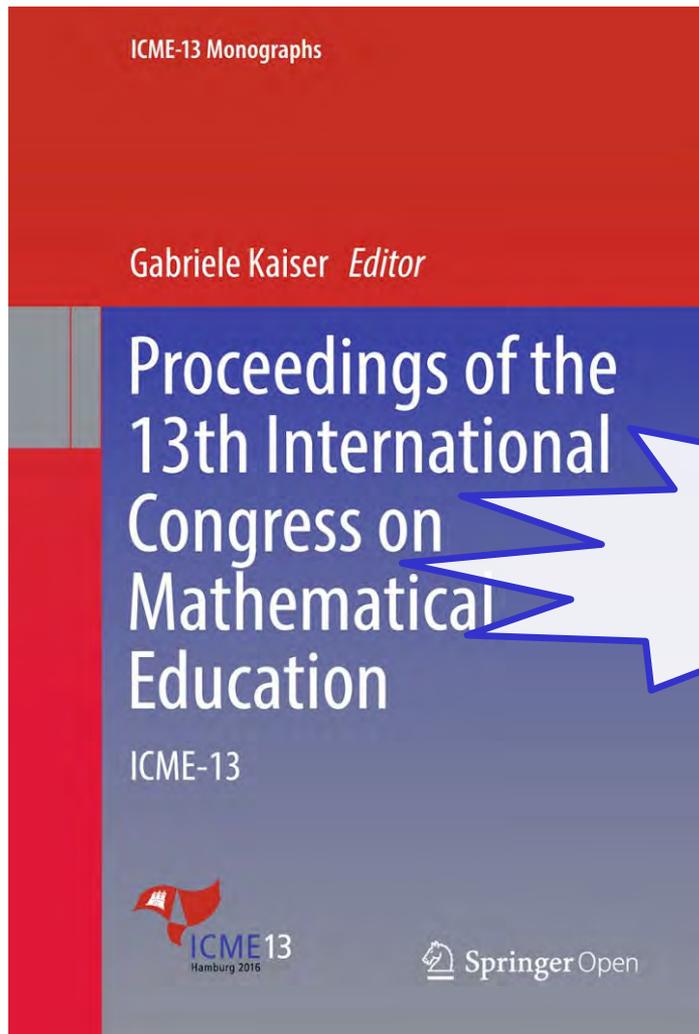
- ✓ 2015-2018: Shigefumi Mori (Fields medallist)



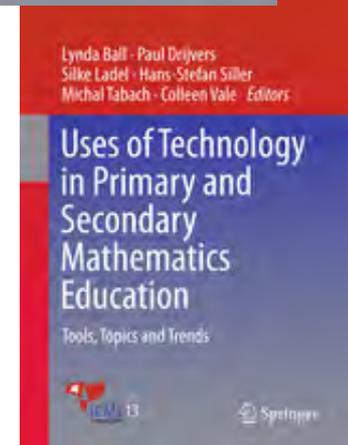
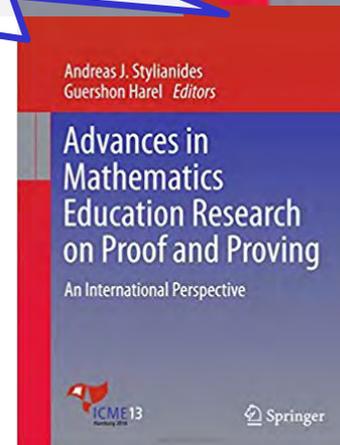
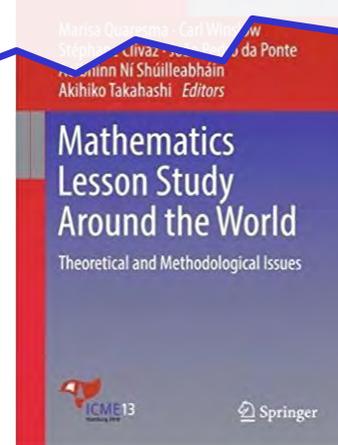
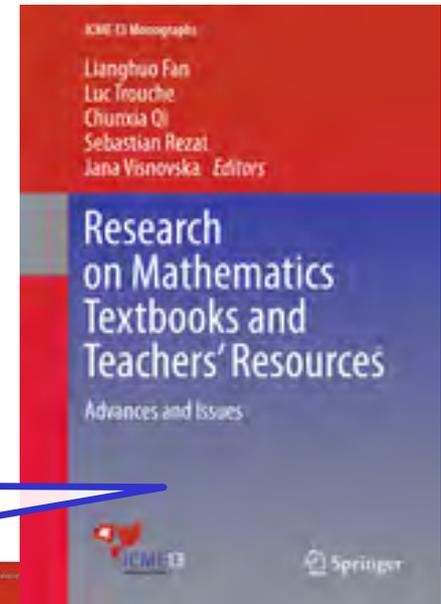
# ICME-13 in Hamburg (Germany)



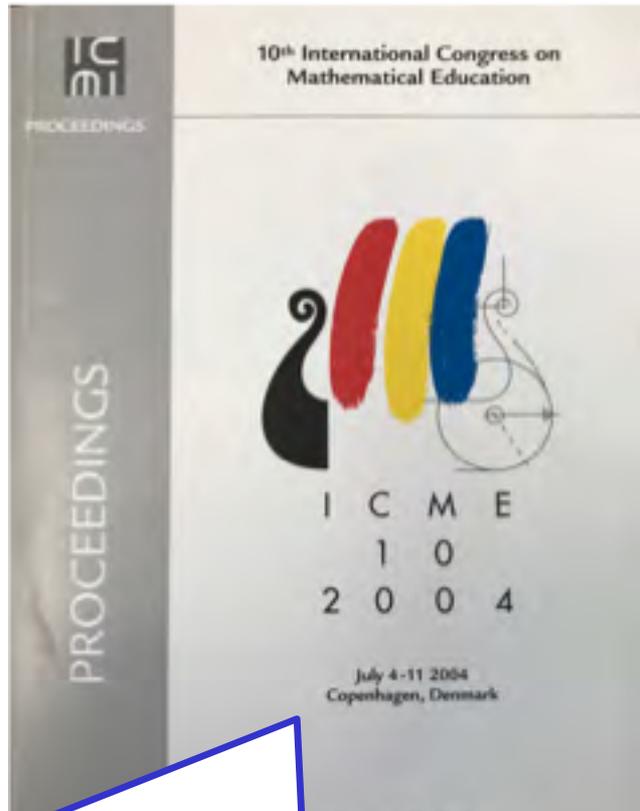
# Proceedings



26 titles !!

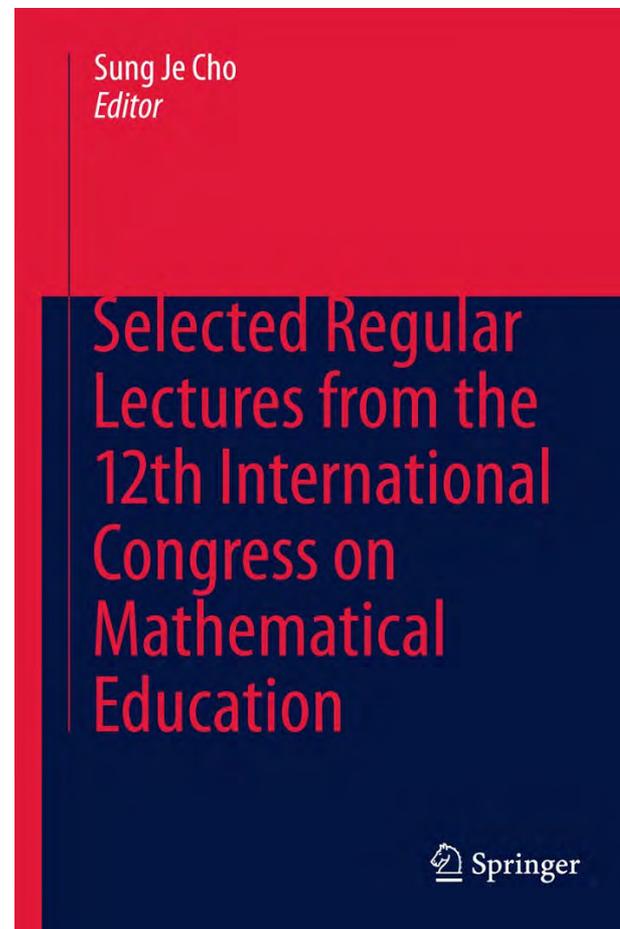
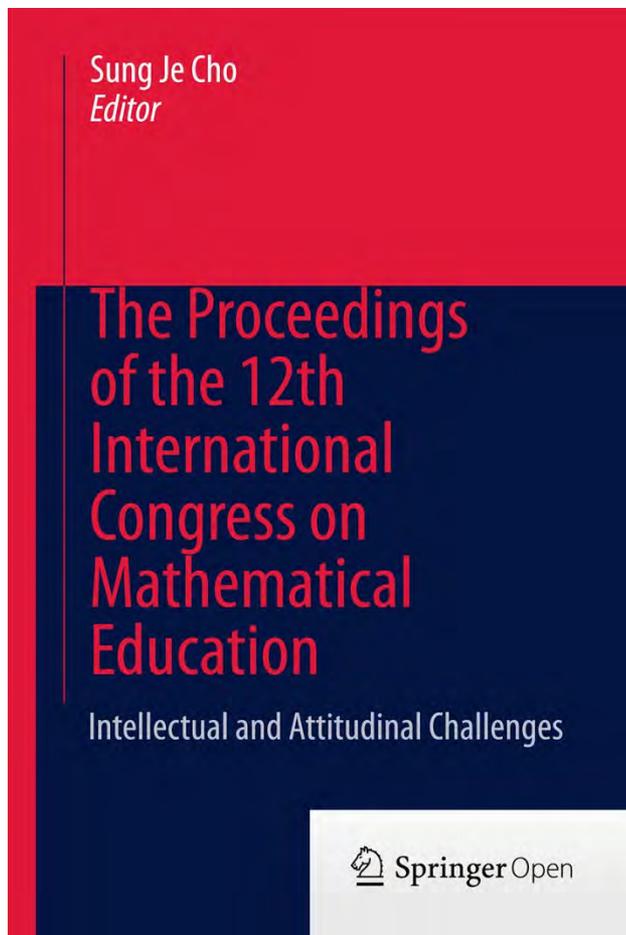


# Evolution of proceedings



ICME-10: Relatively longer papers for plenary activities and short reports from TSG, DG, etc.

# ICME-12 in Seoul (South Korea)



# Towards ICME-14, in Shanghai, 2020

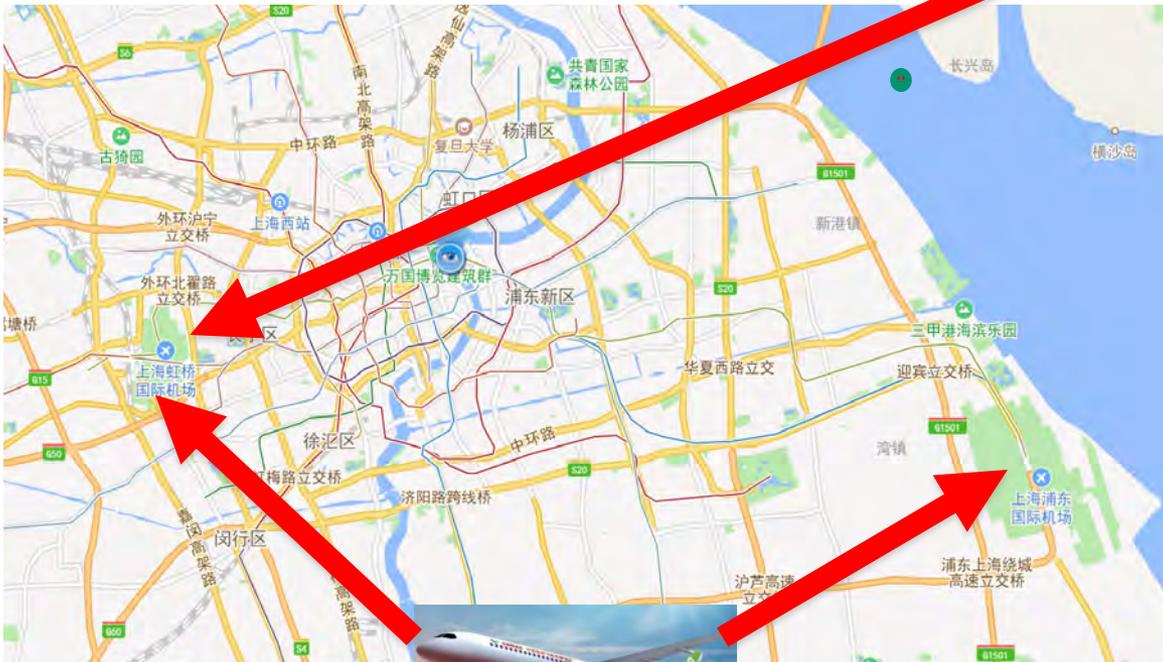
# Towards ICME-14, in Shanghai, 2020

- Basic data of ICME 14, 2020, Shanghai
- Retrospect of bidding for ICME 14
- First IPC meeting
- Topic Study Groups at ICME 14
- Discussion Group / Workshop / National Presentation and others
- Cultural and social activities in Shanghai

# Basic data of ICME 14, 2020, Shanghai

**When:** July 12 to 19, 2020, Shanghai, China

**Where:**



# Basic data of ICME 14, 2020, Shanghai

Website ICME-14: [www.icme14.org](http://www.icme14.org)



The screenshot shows the homepage of the 14th International Congress on Mathematical Education (ICME-14) website. The header features the ICME-14 logo, the title "14<sup>th</sup> International Congress on Mathematical Education", and the dates "July 12 to 19, 2020 Shanghai, China". Below the header is a large banner image of the Shanghai skyline with the text "Shanghai: A view from the Past". The navigation menu includes "HOME" and "LOGIN" buttons, and language options for "中文" and "English". The main content area is titled "Address of Welcome" and contains a text block and a portrait of the congress chair. The text block reads: "As the congress chair of ICME-14, I cordially invite all to participate in the congress to be held in Shanghai from July 12th to 19th, 2020. China is an ancient country with a 5,000-year history of civilization and a brilliant history of mathematics and mathematics education. In recent 100 years, the introduction of western mathematics and mathematics education and their integration with traditional Chinese culture and education have fostered new achievements in mathematics education of modern China. Shanghai, a famous metropolis in the Far East, is the engine for the economic and social development of China and a window of China's opening-up policy. In addition, it is also the cradle of modern Chinese mathematics and mathematics education and the birthplace of the Chinese Mathematical Society. East China Normal University is one of the top universities in China and takes the lead in the development of teacher education in China. The mathematics education team of ECNU has a great influence both at home and abroad. Taking consideration of all these facts, I believe that the ICME-14 hosted in Shanghai will be a grand academic congress and a great surprise for the colleagues around the world. I am very much looking forward to seeing you at ICME-14 in Shanghai and am sure that your participation will contribute to the success of the ICME-14."

Please visit the official ICME-14 website for further information. In the near future you will find a lot of useful information about the important aspects of the upcoming congress.

# Retrospect of bidding for ICME 14

- East China Normal University plays the main role in the bidding**  
The official bidding body is Chinese Mathematical Society (CMS). Authorized by CMS, East China Normal University (ECNU) undertakes the bidding, and also pays the main role in the preparing and hosting ICME 14.
- East China Normal University** is one of the most prestigious universities in China.



# Retrospect of bidding for ICME 14

- **The mathematics education team of ECNU**

ECNU takes the lead in the development of teacher education in China, and has a tradition of laying great emphasis on the practice and research in mathematics education.

The biggest team of mathematics educators in the university in China (8+6+X):

- From the School of Mathematics Science: 5 full professors + 4 associate professors + young potential researchers
- From the School of Education: 3 full professors + 2 associate professors + young potential researchers



# Retrospect of bidding for ICME 14

- **The mathematics education team of ECNU**

ECNU boast an active team of young and middle aged mathematical educators, not only deeply involved in the international mathematics education community, but also outstanding in the research and teaching practices in the field.

There are intensive collaboration with international researchers or research groups, for example, IFE (Lucs group), University of Haifa, University of Delaware, University of Hamburg



# Retrospect of bidding for ICME 14

- **The mathematics education team of ECNU**

The mathematics education team of ECNU has a great influence both at home and abroad.

Prof. Dianzhou Zhang, Jianpan Wang, Binyan Xu from ECNU ever served and is serving as ICMI EC members.

The mathematical educators in ECNU have played active roles in last few ICME, The team successfully host the Third ICMI East Asia Regional Conference on Mathematical Education (EARCOME 3) in 2005.

The team has also successfully organized the ICM 2002 Satellite Conference on Mathematical Education in Lhasa, China,

The team led the national presentation in ICME 11 in Mexico.

# Retrospect of bidding for ICME 14

- **Why ICME 14 in Shanghai**

Shanghai is the engine for the economic and social development of China and a window of China's open-door policy. Since mid-19<sup>th</sup> century, Shanghai has been an important city featuring frequent exchanges between eastern and western culture.

**History:** As early as in the 16<sup>th</sup> century A.D., from Shanghai came a knowledgeable scientist Guangqi Xu (als known as Kwangke Seu) who, together with Metteo Ricci, translated the first six books of Euclid's Elements into Chinese.



# Retrospect of bidding for ICME 14

- **Why ICME 14 in Shanghai**

Nowadays: Shanghai is an important base for mathematics research and education in China.

Data from Shanghai Statistical Yearbook 2013:

| Institutions                 | Students |
|------------------------------|----------|
| 67 Higher learning           | 506,600  |
| 761 primary schools          | 760.400  |
| 871 middle schools           | 736,100  |
| 29 special education schools | 1600     |

# Retrospect of bidding for ICME 14

- **Why ICME 14 in Shanghai**

In recent years, the outstanding performance of Shanghai students in PISA tests has attracted worldwide attention. Shanghai experiences of mathematics education was summarized.

It included mainly:

- the continuity of principles of curriculum reform which combine students' development autonomy and teachers' guidance role;
- the open culture of mathematics classroom teaching, “教无定法”(teaching with various or flexible approaches);
- collective teachers' community

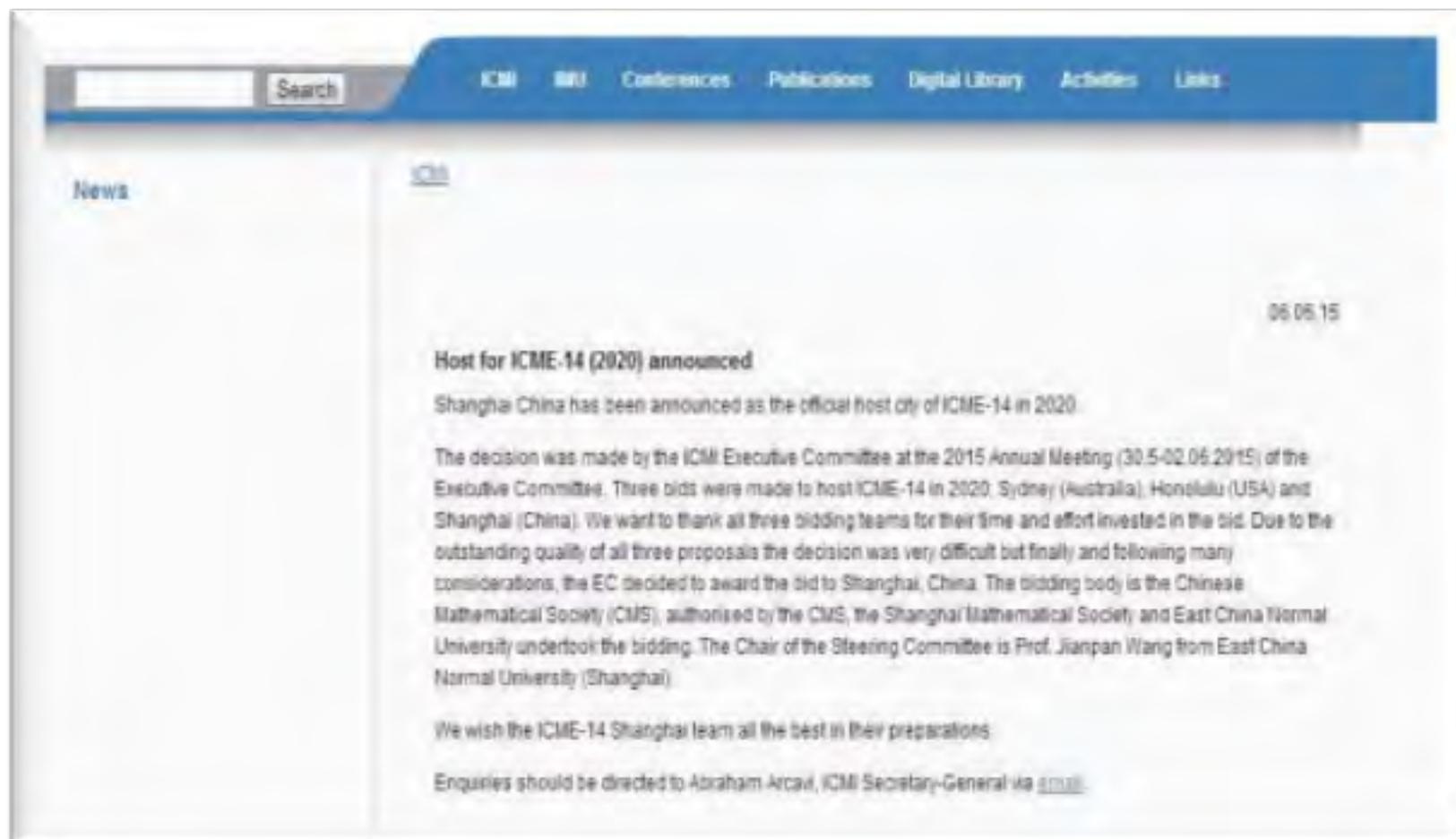
# Retrospect of bidding for ICME 14

- Preparation started in June 2013...
- May, 2015, field defense in East China Normal University



# Retrospect of bidding for ICME 14

- June 6, 2015, announcement by ICMI



The screenshot shows the ICMI website's news section. The header includes a search bar and navigation links for ICMI, IMU, Conferences, Publications, Digital Library, Activities, and Links. The main content area features a news article titled "Host for ICME-14 (2020) announced" dated 06.06.15. The article text states that Shanghai, China has been announced as the official host city of ICME-14 in 2020. It details the decision made by the ICMI Executive Committee at the 2015 Annual Meeting (30.5-02.06.2015) of the Executive Committee, where three bids were made to host ICME-14 in 2020: Sydney (Australia), Honolulu (USA), and Shanghai (China). The article notes that the decision was very difficult due to the outstanding quality of all three proposals. The bidding body is the Chinese Mathematical Society (CMS), authorized by the CMS, the Shanghai Mathematical Society, and East China Normal University. The Chair of the Steering Committee is Prof. Jianpan Wang from East China Normal University (Shanghai). The article concludes with a wish for the ICME-14 Shanghai team and a note that enquiries should be directed to Abraham Arcavi, ICMI Secretary-General via email.

# Retrospect of bidding for ICME 14

- July 2016, to sign the agreement with ICMI EC in Hamburg



# Retrospect of bidding for ICME 14

- July 2016, Welcome speech at the closing of ICME 13 in Hamburg



# First IPC meeting in Shanghai

|                     | Name  | University & Country                                   | Remark                                    |
|---------------------|---|--|---|
| <b>Chair</b>        | Jianpan Wang  | East China Normal University, China                    | ICME-14 Congress Chair                    |
| <b>Members</b>      | Jill Adler  | University of the Witwatersrand, South Africa          | Ex-officio member, ICMI President         |
|                     | Abraham Arcavi                                      | Weizmann Institute of Science, Israel                  | Ex-officio member, ICMI Secretary General |
|                     | Jiansheng Bao                                       | East China Normal University, China                    | ICME-14 LOC Co-chair                      |
|                     | Daniel Chazan                                       | University of Maryland, USA                            |   |
|                     | Faïza Chellougui                                    | University of Carthage, Tunisia                        |   |
|                     | Marta Civil   | University of Arizona, USA                             |   |
|                     | Alicia Dickenstein                                  | Universidad de Buenos Aires, Argentina                 | IMU Vice-President                        |
|                     | Yufeng Guo  | Beijing Normal University, China                       |   |
|                     | Anjum Halai   | Aga Khan University, Pakistan/Tanzania                 |   |
|                     | Gabriele Kaiser                                     | University of Hamburg, Germany                         | ICME-13 Convenor & IPC Chair              |
|                     | Caroline Lajoie                                     | Université du Québec à Montréal, Canada                |   |
|                     | Celi Espasandin Lopes                               | Universidade Cruzeiro do Sul, Brazil                   |   |
|                     | Tomas Lowrie  | University of Canberra, Australia                      |   |
|                     | Maria Alessandra Mariotti                           | Università di Siena, Italy                             |   |
|                     | Takeshi Miyakawa                                    | Joetsu University of Education, Japan                  |   |
|                     | Frode Rønning                                       | Norwegian University of Science and Technology, Norway |   |
|                     | Ewa Swoboda   | Poznań University, Poland                              |   |
| Luc Trouche         | École Normale Supérieure de Lyon, France            |  |   |
| Catherine Vistro-Yu | Ateneo de Manila University, Philippines            |  |   |
| Binyan Xu           | East China Normal University, China                 | ICME-14 LOC Co-chair                                   |   |
| Ivan Yashchenko     | Moscow Center for Continuous Math Education, Russia |  |   |

# First IPC meeting in Shanghai



# First IPC meeting in Shanghai

## Function of IPC

- To determine the overall structure of ICME 14
- To nominate plenary lecturers
- To propose the themes and teams of plenary panels
- To nominate invited lecturers
- To propose themes and teams of survey teams

All these activities will give an overview of the state-of-the-art within mathematics education worldwide, and in addition will provide the participants with insights into present and future major trends in mathematics education.

- To propose Topic study groups

Topic Study Groups will enable the conference participants to actively participate via their own contributions.

# Topic Study Groups at ICME 14

A Topic Study Group (TSG) is designed to gather a group of congress participants who are interested in a particular topic in mathematics education. Topic Study Groups will therefore promote the discussion of a variety of perspectives on the theme of the Group.

| No. | Topic   |
|-----|---|
| 1   | Mathematics education at preschool level              |
| 2   | Mathematics education at tertiary level               |
| 3   | Mathematics education for gifted students             |
| 4   | Mathematics education for students with special needs |
| 5   | Teaching and learning of number and arithmetic        |
| 6   | Teaching and learning of algebra at primary level     |
| 7   | Teaching and learning of algebra at secondary level   |
| 8   | Teaching and learning of geometry at primary level    |
| 9   | Teaching and learning of geometry at secondary level  |
| 10  | Teaching and learning of measurement                  |
| 11  | Teaching and learning of probability                  |
| 12  | Teaching and learning of statistics                   |
| 13  | Teaching and learning of calculus                     |
| 14  | Teaching and learning of programming and algorithms   |
| 15  | Teaching and learning of discrete mathematics         |

# Topic Study Groups at ICME 14

|    |  |
|----|--|
| 16 | Reasoning, argumentation and proof in mathematics education  |
| 17 | Problem posing and solving in mathematics education  |
| 18 | Students' identity, motivation and attitudes towards mathematics and its study                                 |
| 19 | Mathematical literacy, numeracy and competency in mathematics education  |
| 20 | Learning and cognition in mathematics (including learning science)   |
| 21 | Neuro science and mathematics education/Cognitive Science  |
| 22 | Mathematical applications and modelling in mathematics education   |
| 23 | Visualization in the teaching and learning of mathematics  |
| 24 | The role and the use of technology in the teaching and learning of mathematics at primary level                |
| 25 | The role and the use of technology in the teaching and learning of mathematics at lower secondary level        |
| 26 | The role and the use of technology in the teaching and learning of mathematics at upper secondary level        |
| 27 | The role of the history of mathematics in mathematics education  |
| 28 | Preservice mathematical teacher education at primary level   |
| 29 | Preservice mathematical teacher education at secondary level   |
| 30 | In-service mathematical teacher education and mathematical teacher professional development at primary level   |
| 31 | In-service mathematical teacher education and mathematical teacher professional development at secondary level |

# Topic Study Groups at ICME 14

|    |   |
|----|---|
| 32 | Knowledge in/for teaching mathematics at primary level                                    |
| 33 | Knowledge in/for teaching mathematics at secondary level                                  |
| 34 | Affect, beliefs, and identity of mathematics teachers                                     |
| 35 | Knowledge and practice of mathematics teacher educator                                    |
| 36 | Research on classroom practice at primary level   |
| 37 | Research on classroom practice at secondary level   |
| 38 | Task design and analysis  |
| 39 | Language and communication in the mathematics classroom                                   |
| 40 | Research and development on mathematics curriculum  |
| 41 | Research and development on textbooks and resources for learning and teaching mathematics |
| 42 | Research and development in assessment in mathematics education                           |
| 43 | Research and development in testing (national and international) in mathematics education |
| 44 | Mathematics and interdisciplinary education   |
| 45 | Mathematics for non-specialist/mathematics as a service subject at tertiary level         |
| 46 | Mathematical competitions and other challenging activities                                |
| 47 | Mathematics education in a multilingual environment                                       |
| 48 | Mathematics education in a multicultural environment                                      |
| 49 | Distance learning, e-learning, and blended learning of mathematics                        |

# Topic Study Groups at ICME 14

|    |   |
|----|---|
| 50 | Mathematics education in and for work; continuous mathematics education including adult education |
| 51 | Mathematics education for ethnic minorities   |
| 52 | Ethno-mathematics   |
| 53 | Equity in mathematics education   |
| 54 | Social and political dimensions of mathematics education  |
| 55 | The history of the teaching and the learning of mathematics                                       |
| 56 | Philosophy of mathematics and mathematics education   |
| 57 | Diversity of theories in mathematics education  |
| 58 | Empirical methods and methodologies in mathematics education                                      |
| 59 | Mathematics and creativity  |
| 60 | Semiotics in mathematics education  |
| 61 | International education cooperation   |
| 62 | Popularization of mathematics   |

# Discussion Group / Workshop / National Presentation and others

- **Discussion groups** are designed to gather congress participants who are interested in **discussing**, in a genuinely interactive way, certain challenging, controversial or emerging issues and dilemmas of interest to an international or regional audience.
- **Workshops** aim for an even deeper **interaction** with a specific topic emphasizing activities of the participants
- **A National Presentation** is an activity during which representatives of a given country will make a presentation on the state and trends in **mathematics education in that country**.

# Cultural and social activities in Shanghai

Shanghai French Concession, since the end of 19th century, ended in 1943.

Shanghai Wu Kang Building (I.S.S Normandie Apartment, constructed since 1924), Xuhui district, Huai Hai Zhong Road



# Cultural and social activities in Shanghai

Shanghai Xuhui district, Hengshan Road (at that time in Shanghai French Concession)



# Cultural and social activities in Shanghai

Fuxing Garden (at that time called French Garden)



# Typical Shanghai visiting

Zhu Jia Jiao, Water village, more than 2000 years old



Welcome to ICME 14  
July 12-19, 2020

Welcome to Shanghai, China



# Current collaborative projects

In the frame of the P<sub>Ro</sub>S<sub>FER</sub> and JoRISS programs, ECNU -ENS de Lyon collaboration



2014-2015 The C2SE project (French-Chinese laboratory for comparing curricula in science education)

<http://joriss.ens-lyon.fr/education-science-c2se--186013.kjsp?RH=JORISS-PROJECTS&RF=1365416327206>

2015-2016 The CORE-M project (Collective and Resources for teaching Mathematics)

2016-2017 The MaTRiTT project (Mathematics teachers' resources in a Time of Transitions)

<http://ife.ens-lyon.fr/ife/recherche/groupes-de-travail/matrirtt-joriss>



Chongyang WANG



Luc TROUCHE



Luxizi ZHANG



Binyan XU



Jiansheng BAO



Fangchun ZHU



Sophie Soury-Lavergne



Jana TRGALOVA



Mingyu SHAO

**Chongyang WANG's** work pays particular interests on the **expertise in teachers' documentation work**, and mathematics teacher professional development in **collective resource work**. In her PhD study, two groups of math teachers from lower secondary schools (one in China and one in France) were followed. She hopes to explore the components of documentation expertise and the mechanism for its development, through the contrasting case studies.

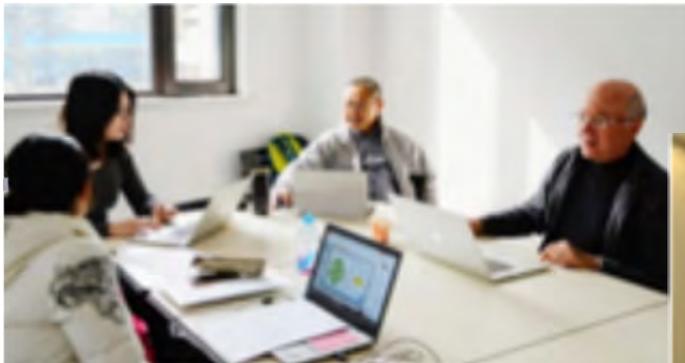
**Fangchun ZHU** focus on the **instrumental orchestration** for mathematics teachers in **dynamic geometry environment**. In the research, he pays attention to one of the special resources: mathematics task with dynamic geometry and analyze the different roles of dynamic geometry in teachers' didactical process. By contrasting french and chinese cases, he wants to analyze the different in the orchestration of different mathematics tasks.



**Luxizi ZHANG** is studying variations in teaching mathematics through the lens of resources.

Comparing the similarities and differences of the variation in Chinese mathematics teaching with that of French. The variation can be the variation of teachers themselves (teachers' documentation work) and the variation of the exercises on the basis of “BIANSHIJIAOXUE” (Bao et al., 2003; Gu et al., 2004), theory of variation (Marton, 2015), didactic variables (Brousseau 1986), and changes of registers (Duval, 2006).

**Mingyu SHAO** is adopting the comparative analysis and the design research methodology, the research will be devoted to describe how (under which condition and by what means) the digital learning environment can promote the learning of analytical geometry concept—in particular, what is the relationship between the development of student thinking level along the hypothetical learning trajectory and the development of student individual instrumental genesis of dynamic geometry software? Theoretical Basis: the notion of hypothetical learning trajectory (Simon, 1995; Clement & Sarama, 2004), instrumental approach (Verillon & Rabardel, 1995) and instrumental genesis (Gueudet & Trouche, 2009).



Wish all of you  
a complete success

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